

APPEAL, Spring-8
7/11/2006

Formation process of Θ^+ inclusive

$\gamma D \rightarrow \Theta^+ X$ reactions

Alexander Titov

RIKEN

and

Joint Institute for Nuclear Research Dubna

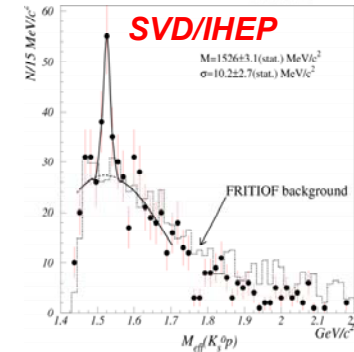
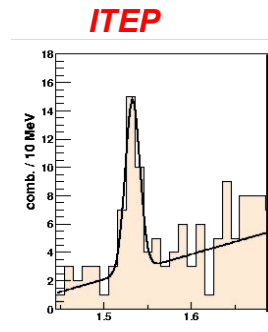
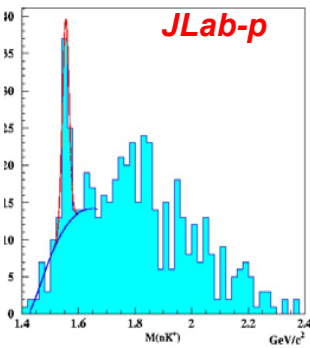
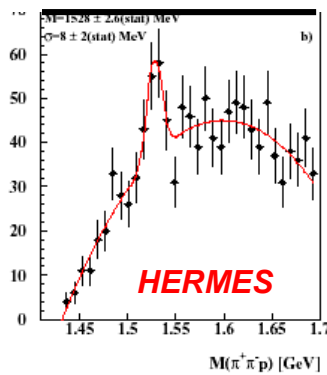
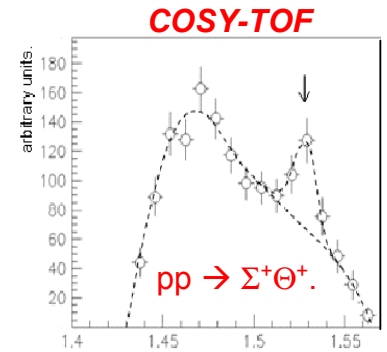
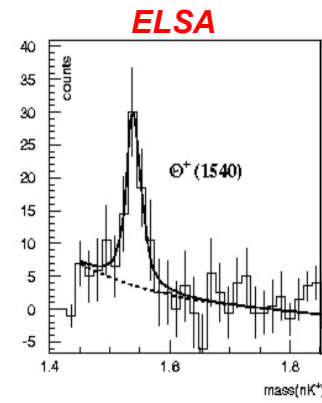
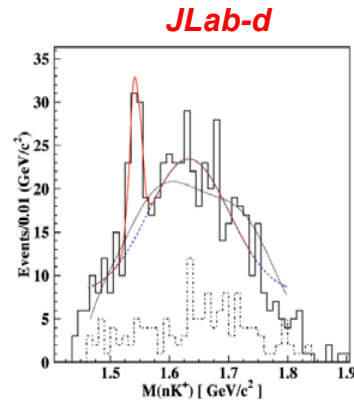
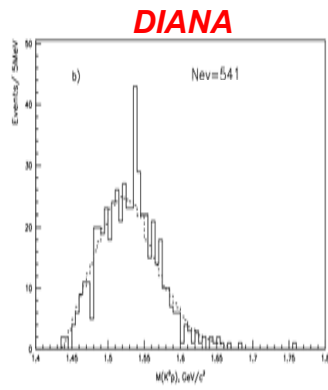
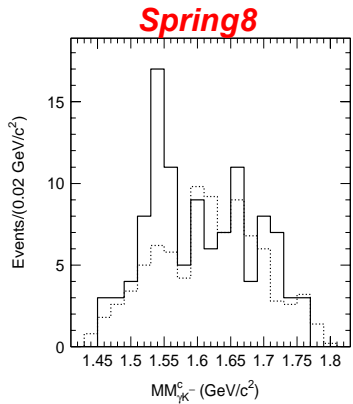
with Burkhard Kämpfer, Schin Daté and Yuji Ohashi

development of
PRC 72, 035206 (2005)

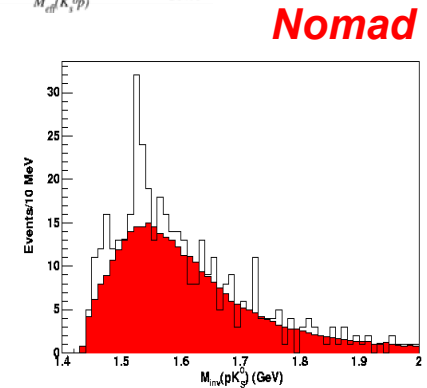
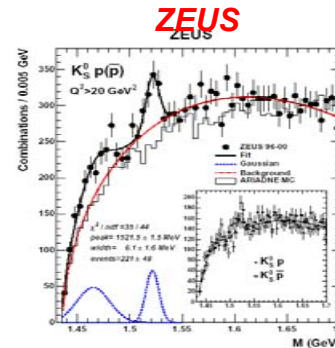
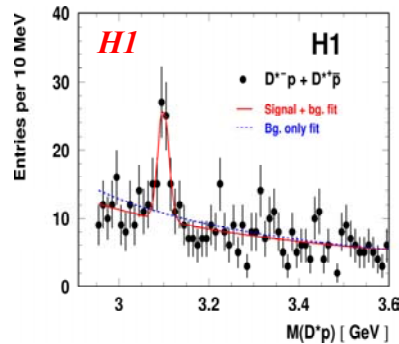
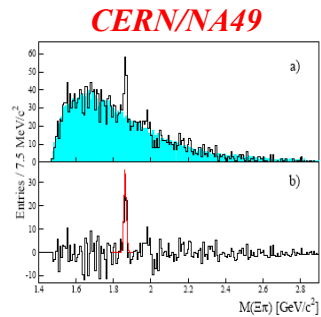
Talk Outline

- **Motivation: is Θ^+ still alive ?**
- **Formation $K + N \rightarrow \Theta^+$ process**
- **Background processes**
- **Results:**
 - **Θ^+ formation at LEPS conditions**
 - **Θ^+ formation at CLAS conditions**
- **Summary**

Evidence for Penta-Quark States



This is a lot of evidence



Experiments on the Θ^+

- Similar number of positive and negative results have been reported.
- But most of the recent ones are negative.

Positive result

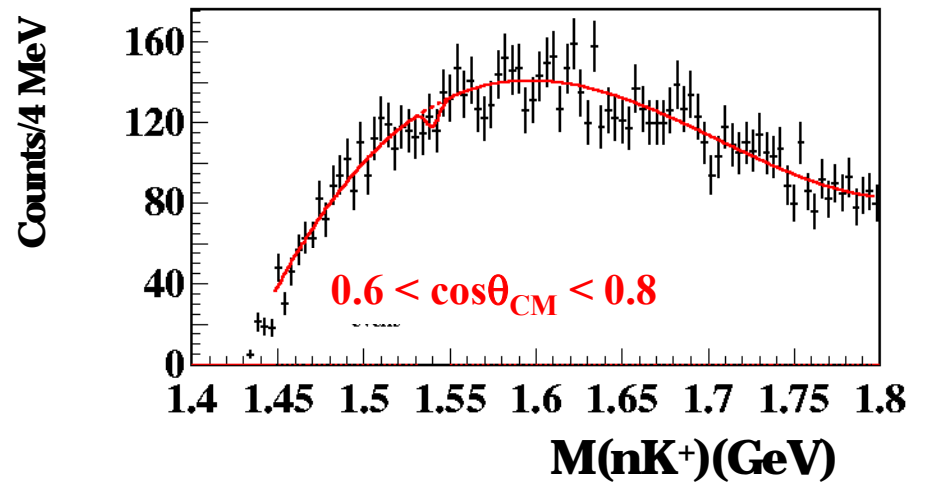
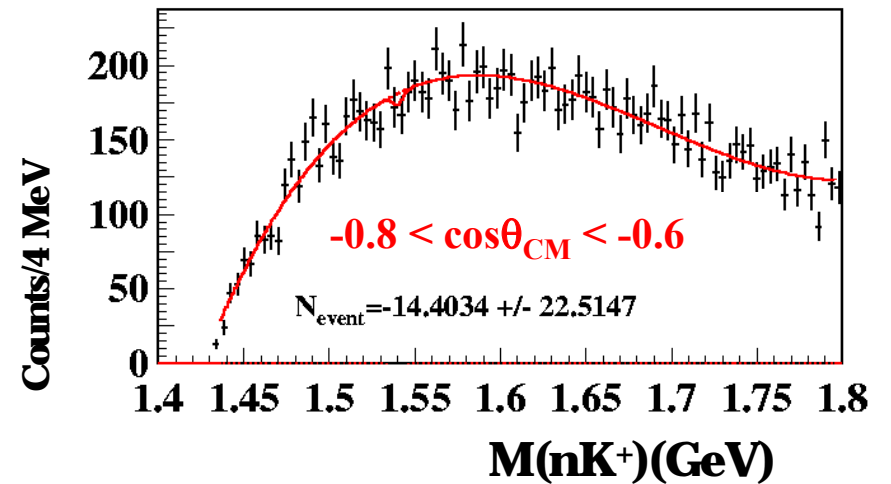
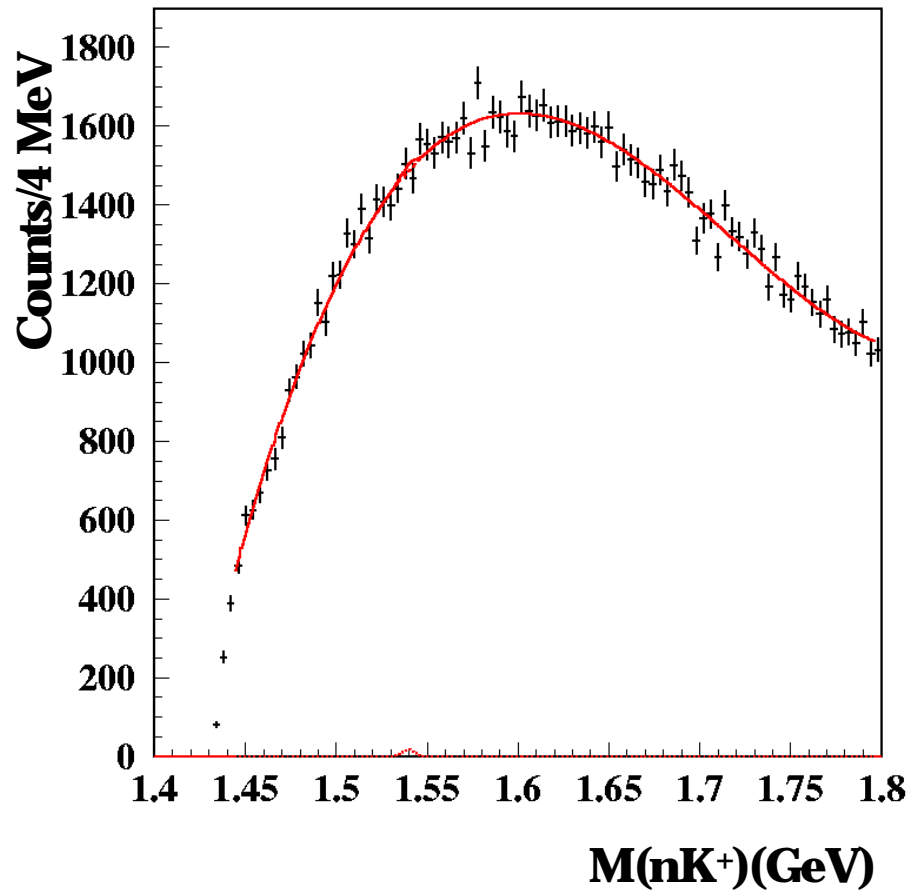
Negative result

Group	Reaction	Mass (MeV)	Group	Reaction
LEPS	$\gamma C \rightarrow K^+ K^- X$	1540 ± 10	BES	$e^+ e^- \rightarrow J/\Psi \rightarrow \Theta \Theta$
DIANA	$K^+ X e \rightarrow K^0 p X$	1539 ± 2	BaBar	$e^+ e^- \rightarrow \Upsilon(4S) \rightarrow p K^0 X$
CLAS	$\gamma d \rightarrow K^+ K^- p(n)$	1542 ± 5	Belle	$e^+ e^- \rightarrow B^0 \bar{B}^0 \rightarrow p \bar{p} K^0 X$
SAPHIR	$\gamma d \rightarrow K^+ K^0(n)$	1540 ± 6	LEP	$e^+ e^- \rightarrow Z \rightarrow p K^0 X$
ITEP	$\nu A \rightarrow K^0 p X$	1533 ± 5	HERA-B	$p A \rightarrow K^0 p X$
CLAS	$\gamma p \rightarrow \pi^+ K^+ K^- (n)$	1555 ± 10	SPHINX	$p C \rightarrow K^0 \Theta^+ X$
HERMES	$e^+ d \rightarrow K^0 p X$	1526 ± 3	HyperCP	$p Cu \rightarrow K^0 p X$
ZEUS	$e^+ p \rightarrow e^+ K^0 p X$	1522 ± 3	CDF	$p \bar{p} \rightarrow K^0 p X$
COSY-TOF	$pp \rightarrow K^0 p \Sigma^+$	1530 ± 5	FOCUS	$\gamma BeO \rightarrow K^0 p X$
SVD	$p A \rightarrow K^0 p X$	1526 ± 5	Belle	$\pi + Si \rightarrow K^0 p X$
			PHENIX	$Au + Au \rightarrow K^- \bar{n} X$

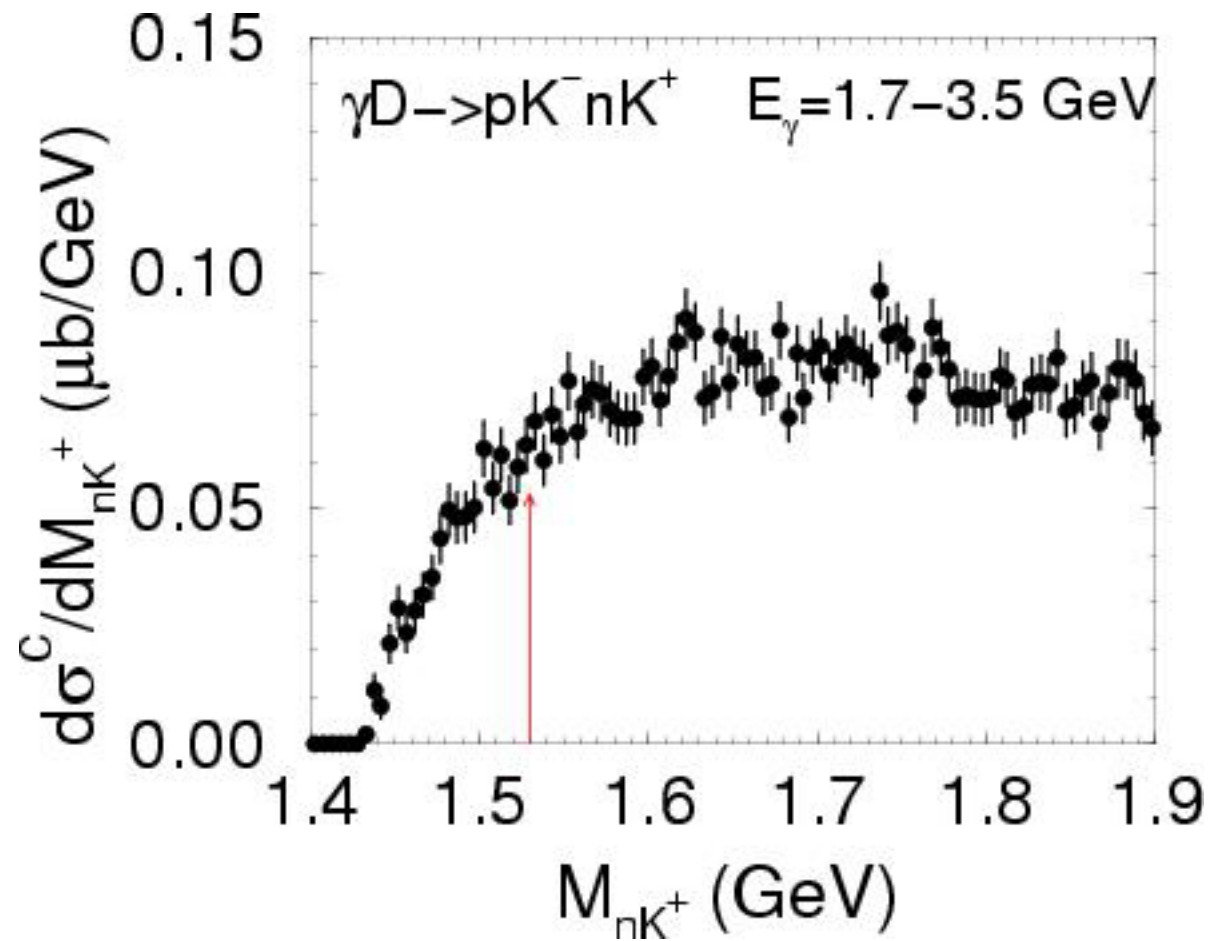
R. De Vita et al,[The CLAS Coll.]

hep-ex/0606062

CLAS: New high statistics exp.
Search for Θ^+ in $\gamma p \rightarrow \Theta^+ K_s \rightarrow K^+ K_s n$

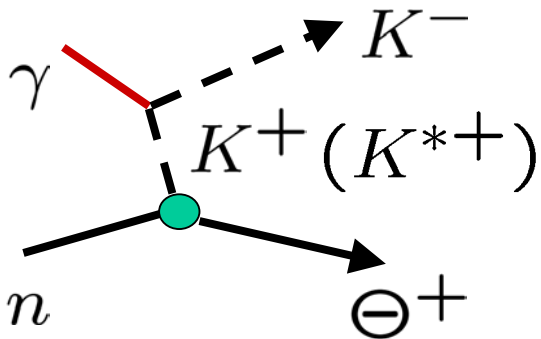


B. McKinnon et al, [The CLAS collaboration]
Phys. Rev. Lett. 96, 212001 (2006)]



Sense of the CLAS new result

Θ^+ photoproduction in elementary
 $\gamma n \rightarrow \Theta^+ K^-$ and $\gamma p \rightarrow \Theta^+ \bar{K}^0$ is suppressed

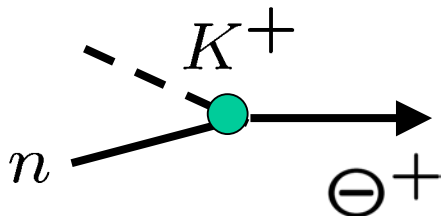


$$T \sim g_{\Theta NK} \times F(p_{K^+}^2)$$

$$g_{\Theta NK} = f(\Gamma_{\Theta})$$

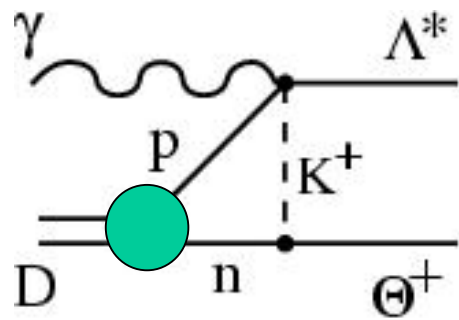
$$F(p^2) = \frac{\Lambda^4}{\Lambda^4 + (M_K^2 - P^2)^2}$$

Search for formation process

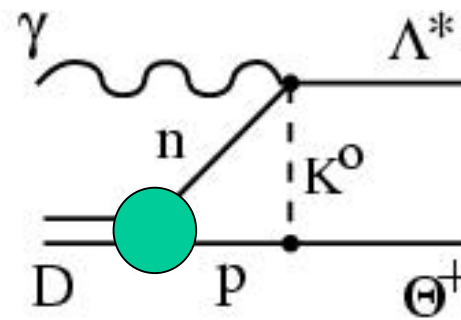


$$T \sim \sqrt{\Gamma_{\Theta}}$$

Associated $\Theta^+ \Lambda^*$ photoproduction

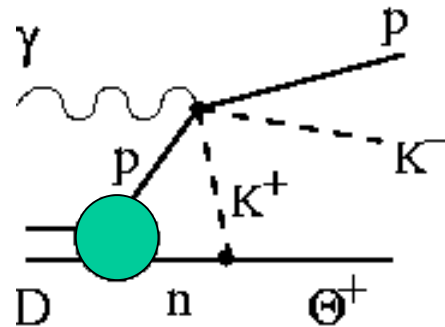


(a)

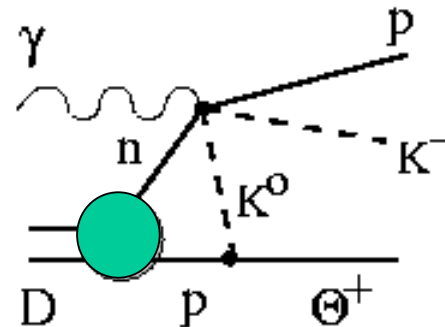


(b)

Associated $\Theta^+ p K^-$ photoproduction



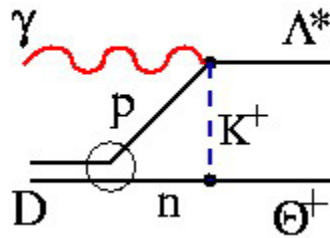
(a)



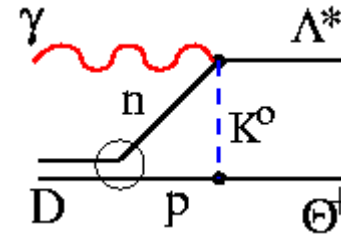
(b)

Two comments

1. interference between

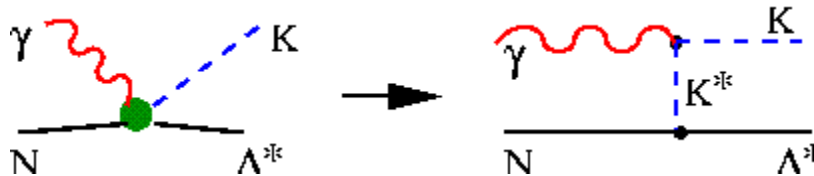


and



is constructive

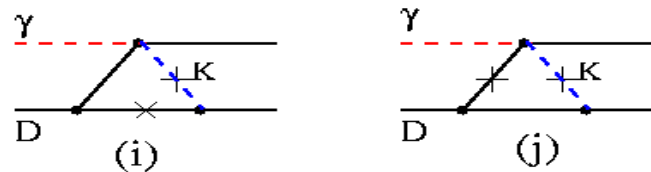
K^* - exchange dominance



$$g_{n\Theta^+K^+} = -g_{p\Theta^+K^0}$$

$$g_{\gamma K^0 K^*} \simeq -\sqrt{2}g_{\gamma K^+ K^*}$$

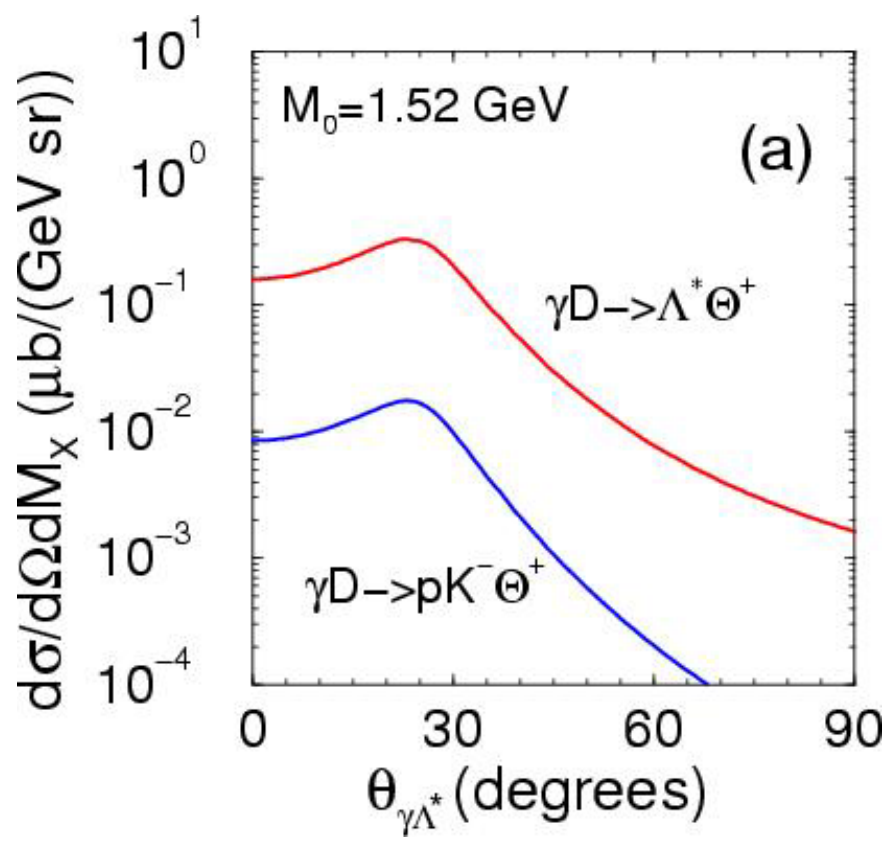
2. main contribution comes from the imaginary parts of three-angle diagrams



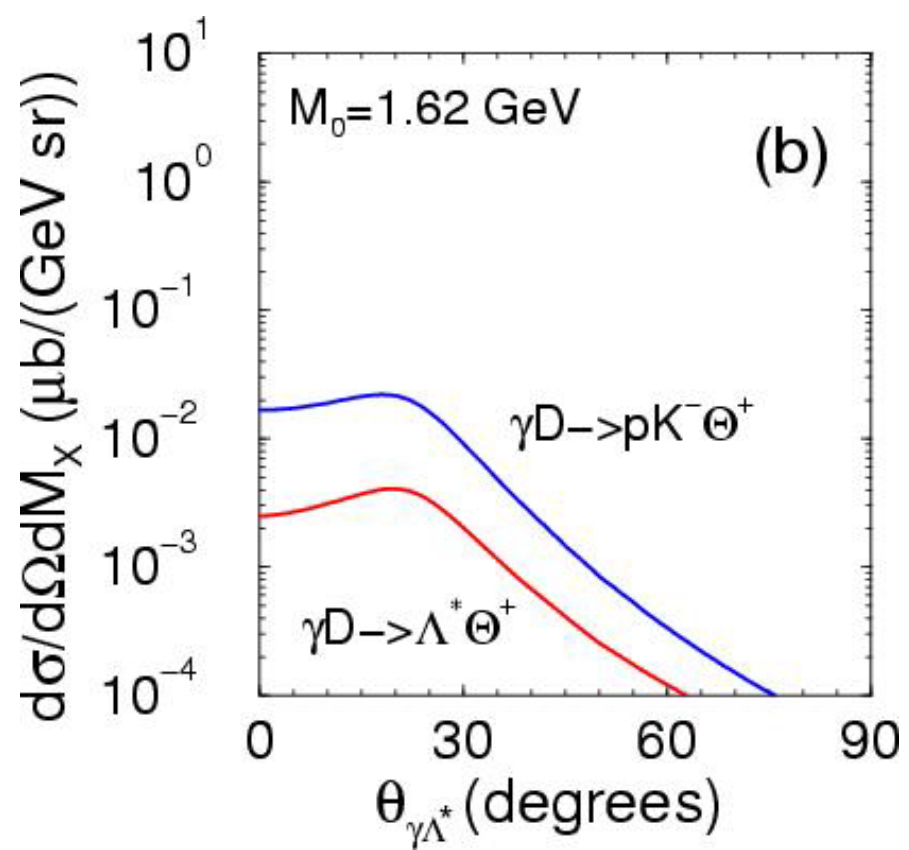
$$\frac{1}{q^2 - M_K^2} \rightarrow 2\pi i \delta(q^2 - M_K^2),$$

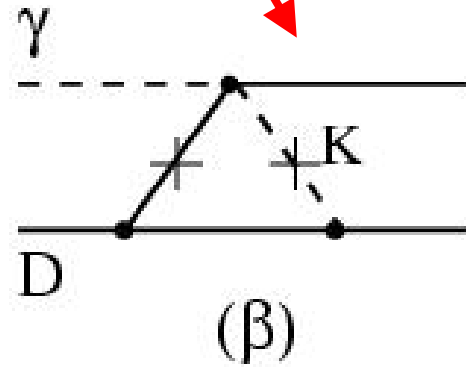
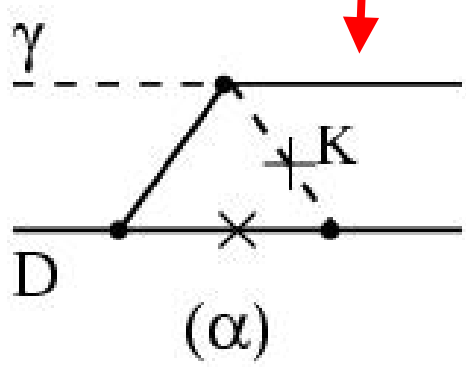
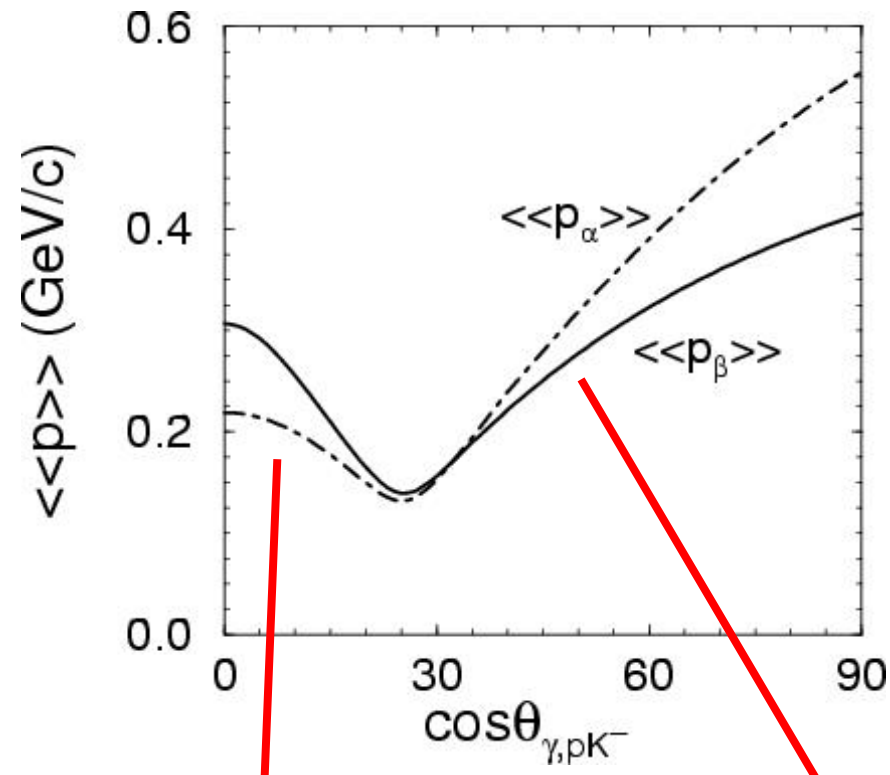
$$\frac{\not{p} + M}{p^2 - M^2} \rightarrow 2\pi i (\not{p} + M) \delta(p^2 - M^2)$$

inside of Λ^*
resonance region

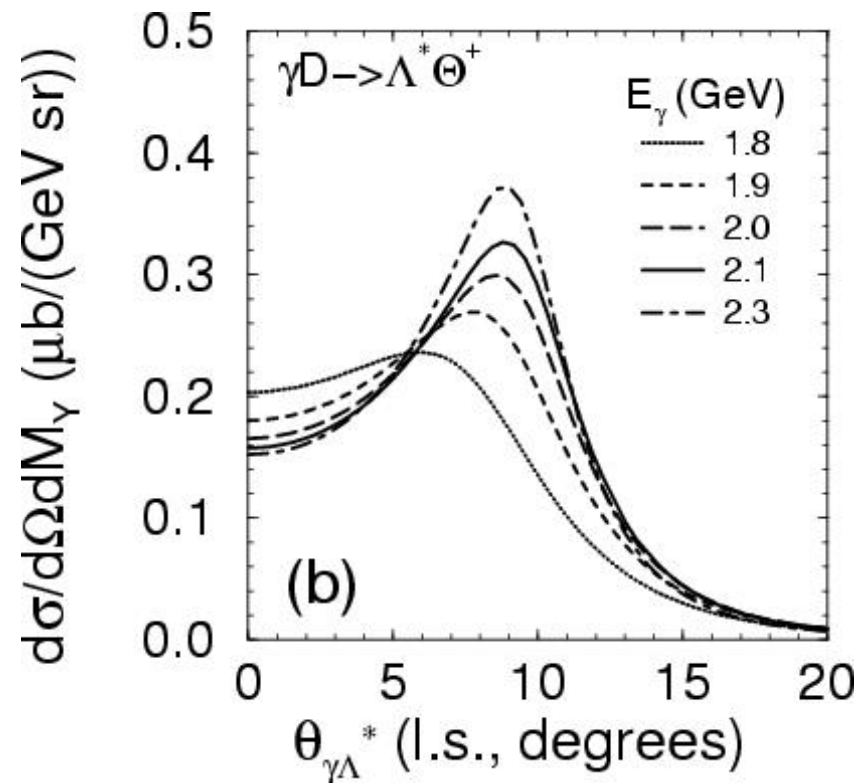
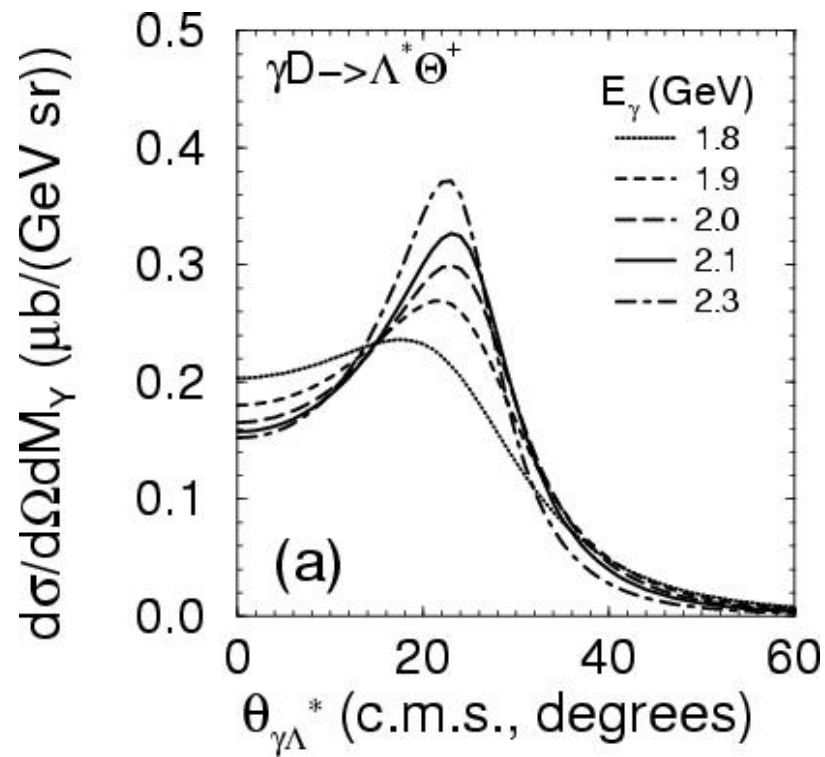


outside of Λ^*
resonance region

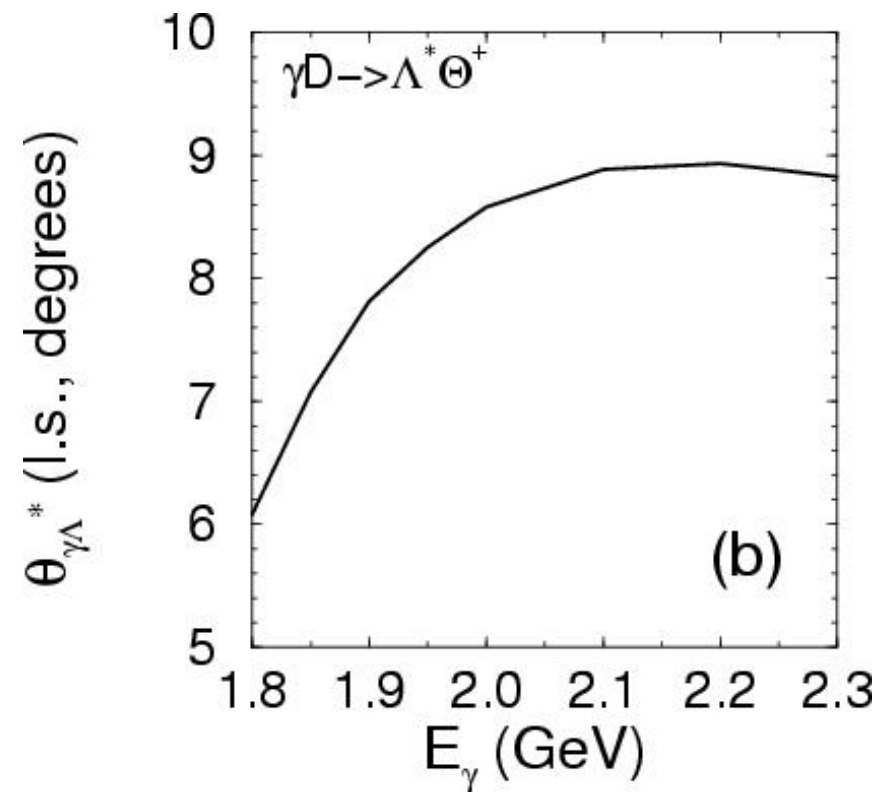
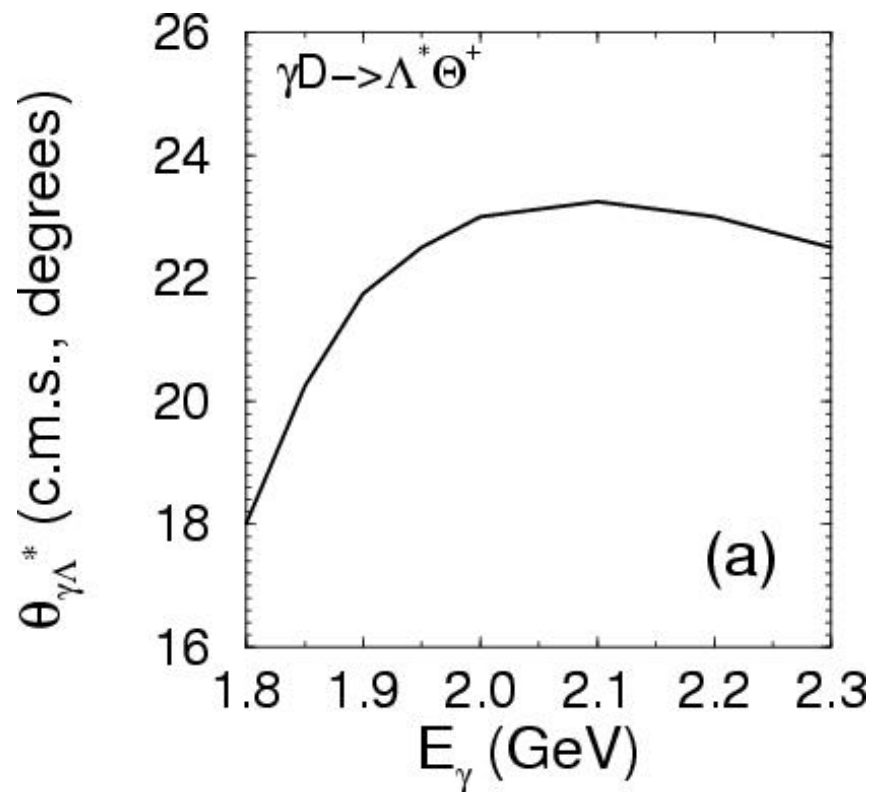




Associated $\Lambda^* \Theta^+$ photoproduction
as a function of Λ^* photoproduction angle



Position of maximum in cross section of the associated $\Lambda^* \Theta^+$ photoproduction as a function of Λ^* photoproduction angle

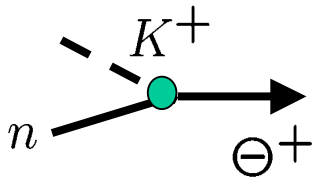


Dependence on Θ^+ spin and parity

$$|g_{\Theta NK}^{\frac{1}{2}\pm}|^2 = \frac{4\pi\Gamma_{\Theta}}{p_F} \frac{M_{\Theta}^2}{(M_{\Theta} \mp M_N)^2 - M_K^2},$$

$$|g_{\Theta NK}^{\frac{3}{2}\pm}|^2 = \frac{48\pi\Gamma_{\Theta}}{p_F} \frac{M_{\Theta}^6}{\lambda(M_{\Theta}^2, M_N^2, M_K^2)((M_{\Theta} \mp M_N)^2 - M_K^2)},$$

$$|g_{\Theta NK}^{\frac{1}{2}-}|^2 : |g_{\Theta NK}^{\frac{1}{2}+}|^2 : |g_{\Theta NK}^{\frac{3}{2}+}|^2 : |g_{\Theta NK}^{\frac{3}{2}-}|^2 = 0.134 : 1 : 1.39 : 10.21 .$$



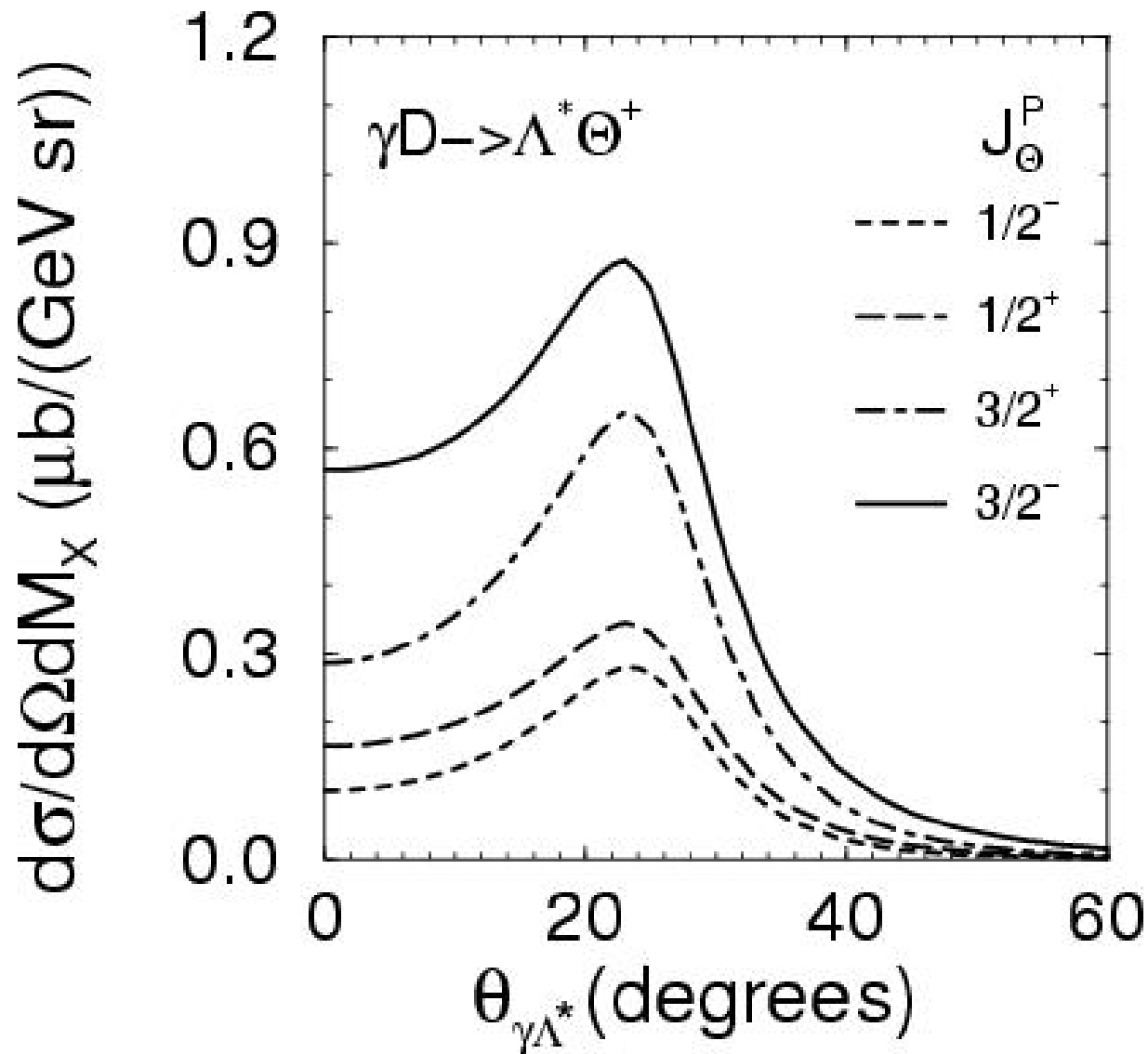
But cross section is proportional to $|A^{JP}|^2$

$$|A^{\frac{1}{2}\pm}|^2 = 8\pi M_{\Theta}^2 \frac{\Gamma_{\Theta} (M_{\Theta} \mp \bar{M}_N)^2 - M_K^2}{p_F (M_{\Theta} \mp M_N)^2 - M_K^2},$$

$$|A^{\frac{3}{2}\pm}|^2 = 16\pi M_{\Theta}^2 \frac{\Gamma_{\Theta} \lambda(M_{\Theta}^2, \bar{M}_N^2, M_K^2) (M_{\Theta} \pm \bar{M}_N)^2 - M_K^2}{p_F \lambda(M_{\Theta}^2, M_N^2, M_K^2) (M_{\Theta} \pm M_N)^2 - M_K^2},$$

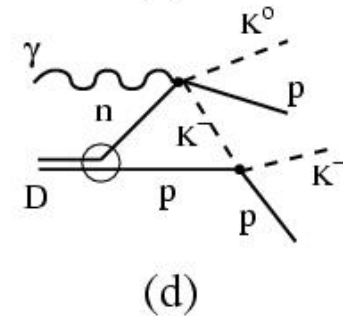
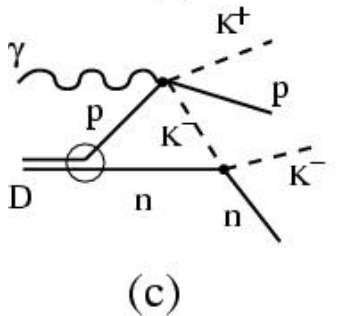
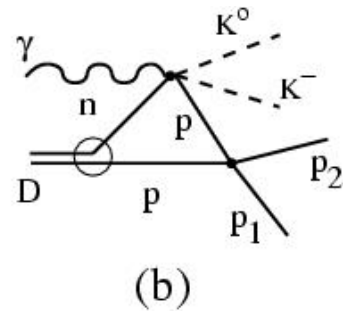
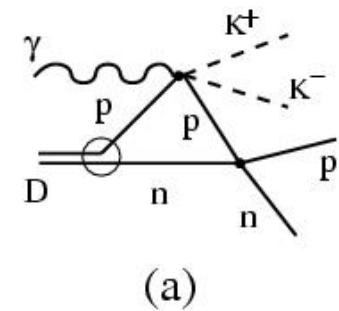
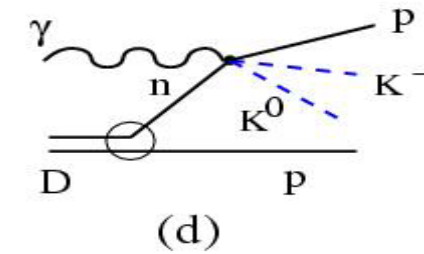
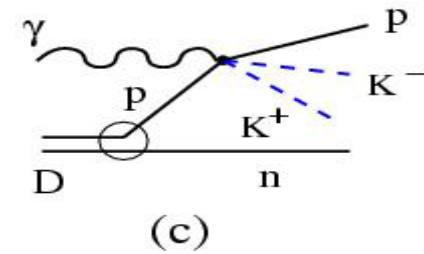
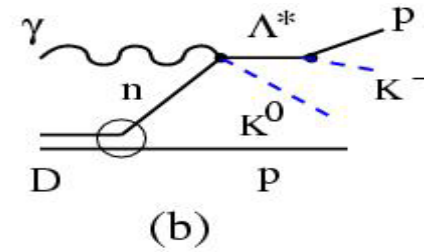
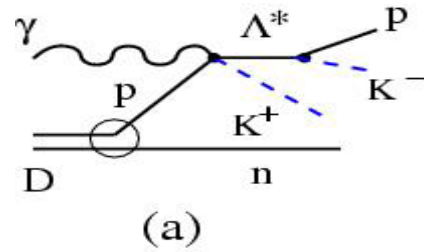
$$\frac{1^-}{2} : \frac{1^+}{2} : \frac{3^+}{2} : \frac{3^-}{2} \simeq 0.8 : 1 : 1.9 : 2.5$$

Dependence on Θ^+ spin and parity



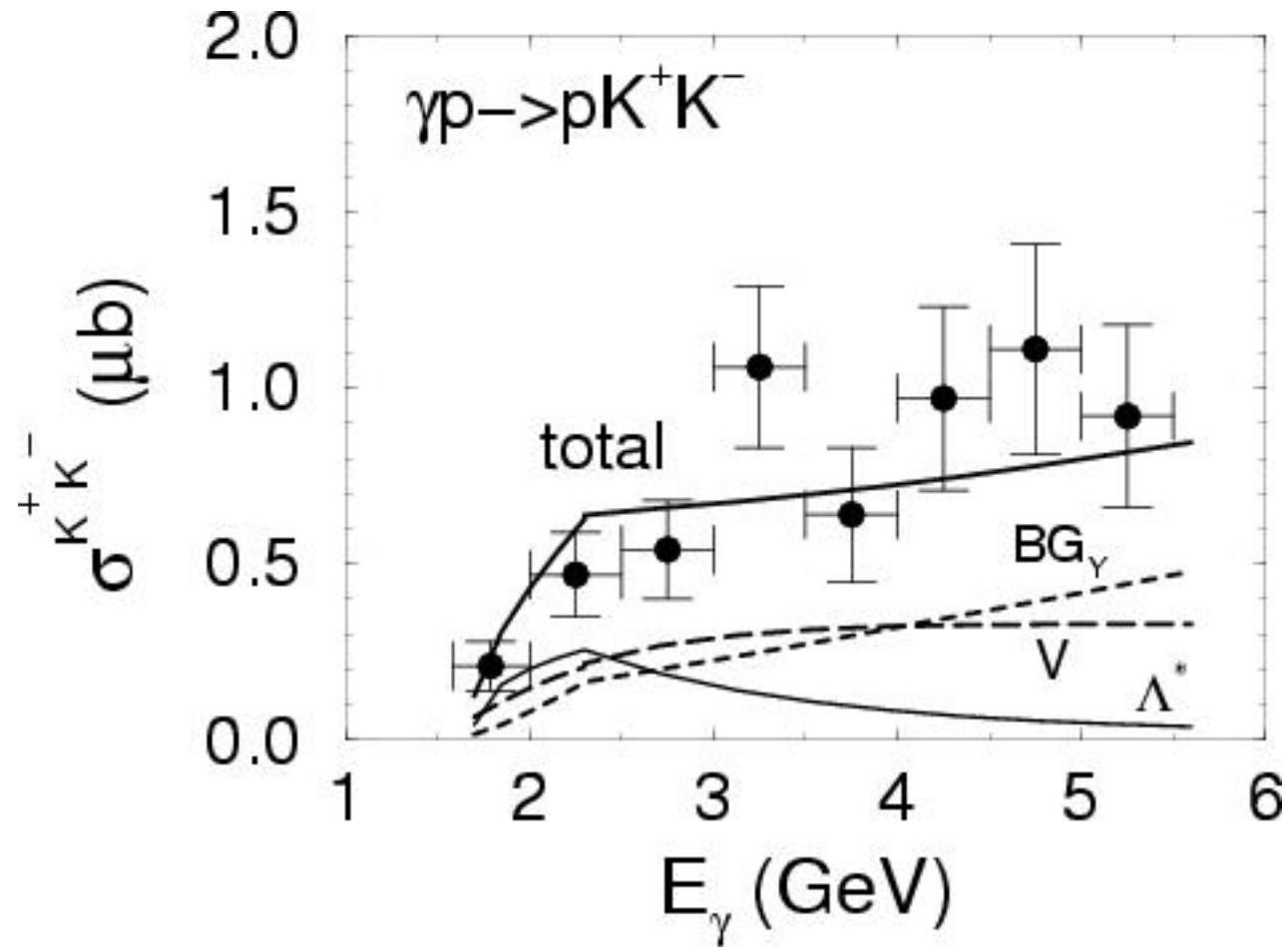
Background

Spectator channels



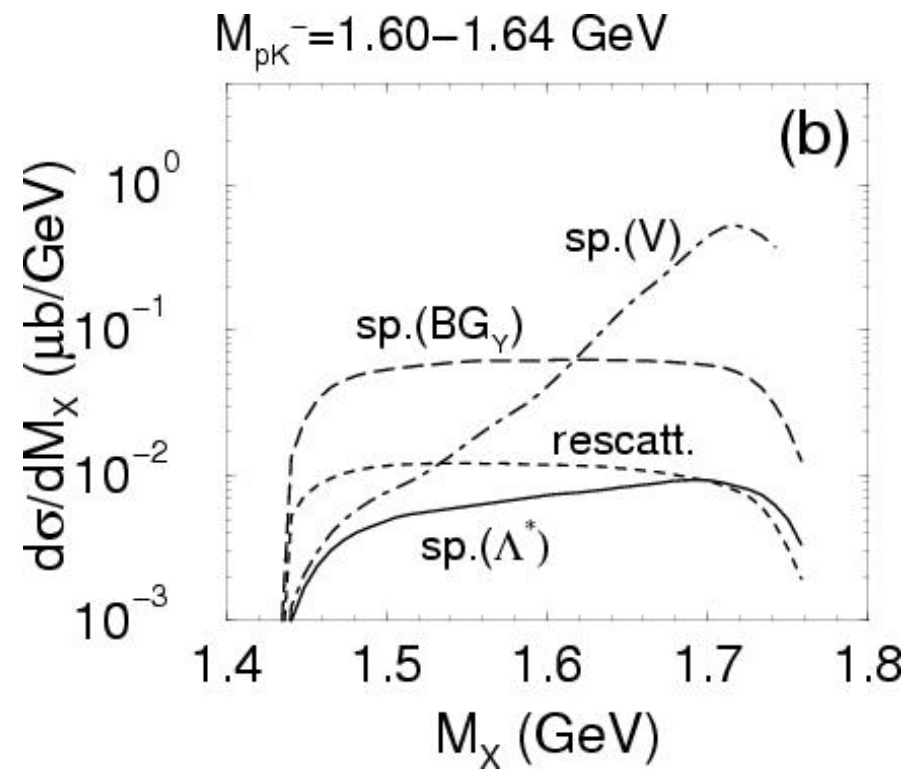
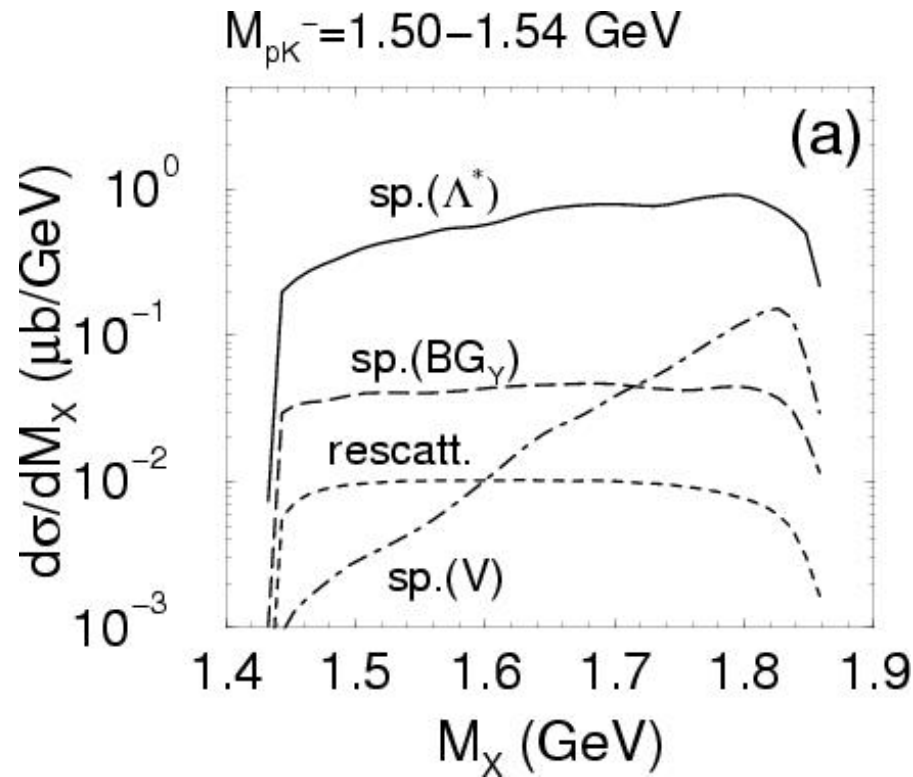
Re-scattering channels

Background: Reaction $\gamma N \rightarrow N \bar{K} K$
total cross section

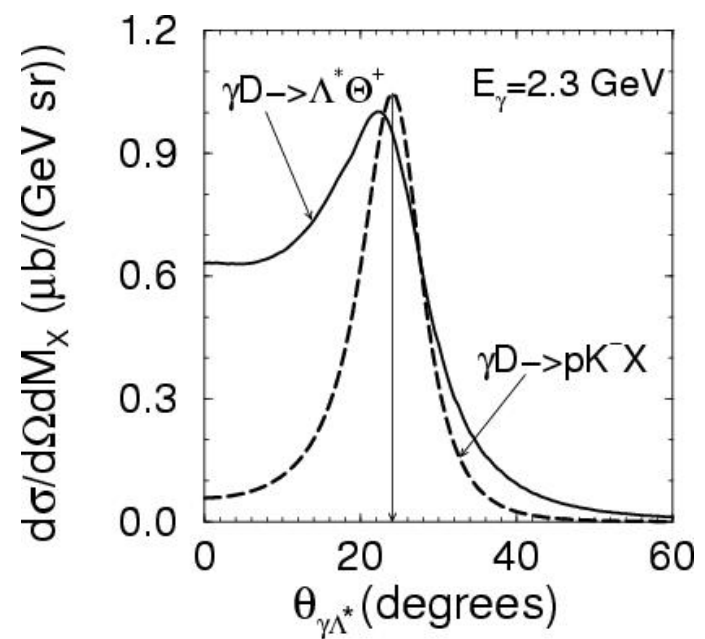
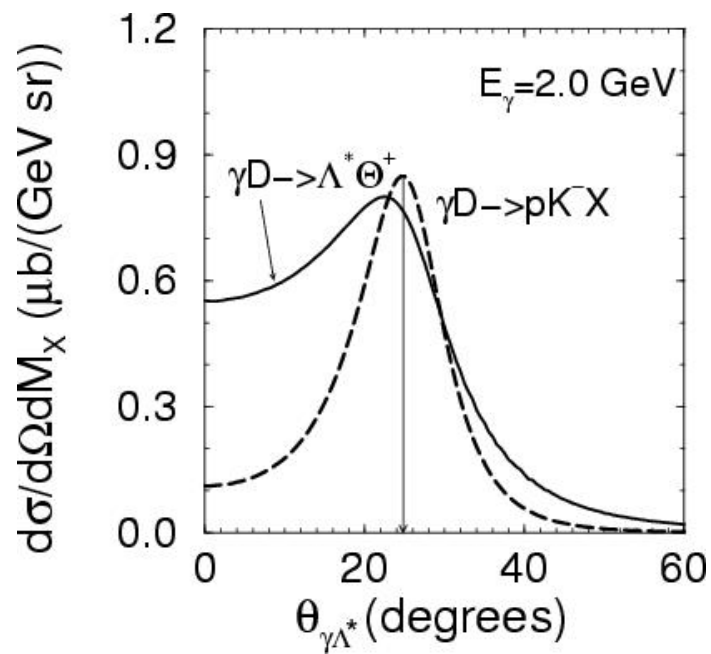


inside of Λ^*
resonance region

outside of Λ^*
resonance region

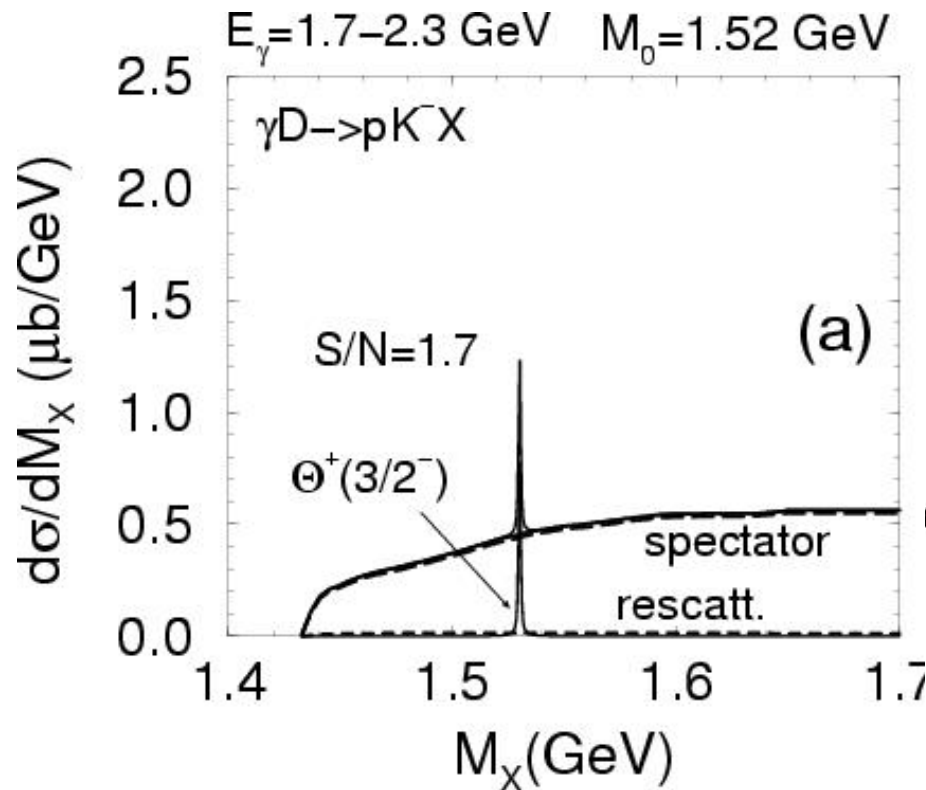


Angular dependence of signal and noise



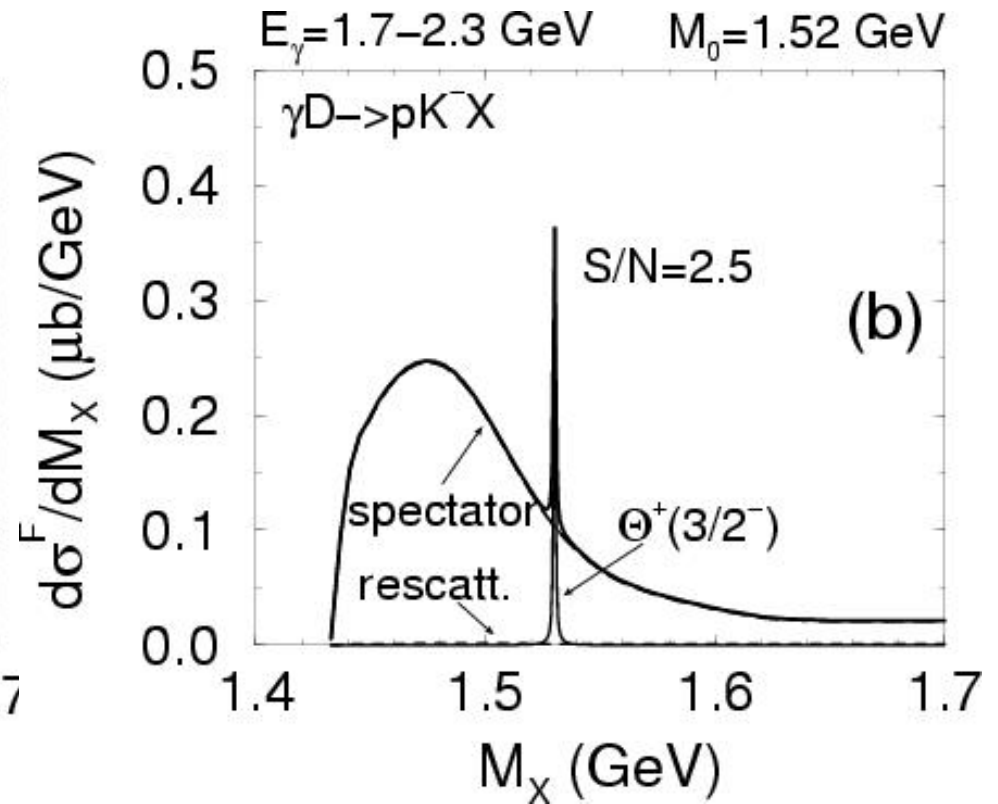
Results for $E_\gamma = 1.7 - 2.3$ GeV (LEPS)

no angle cut

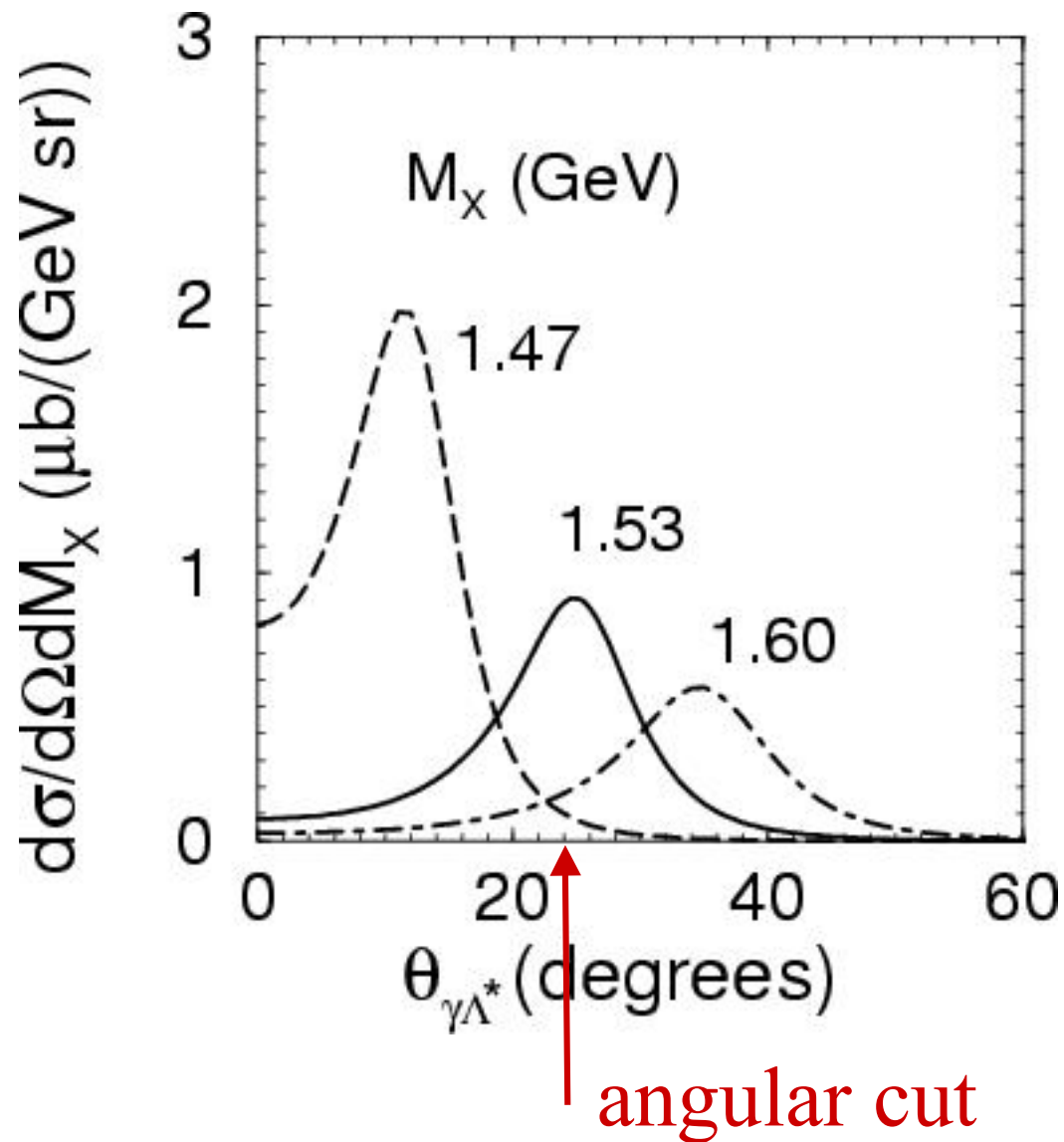


with angle cut

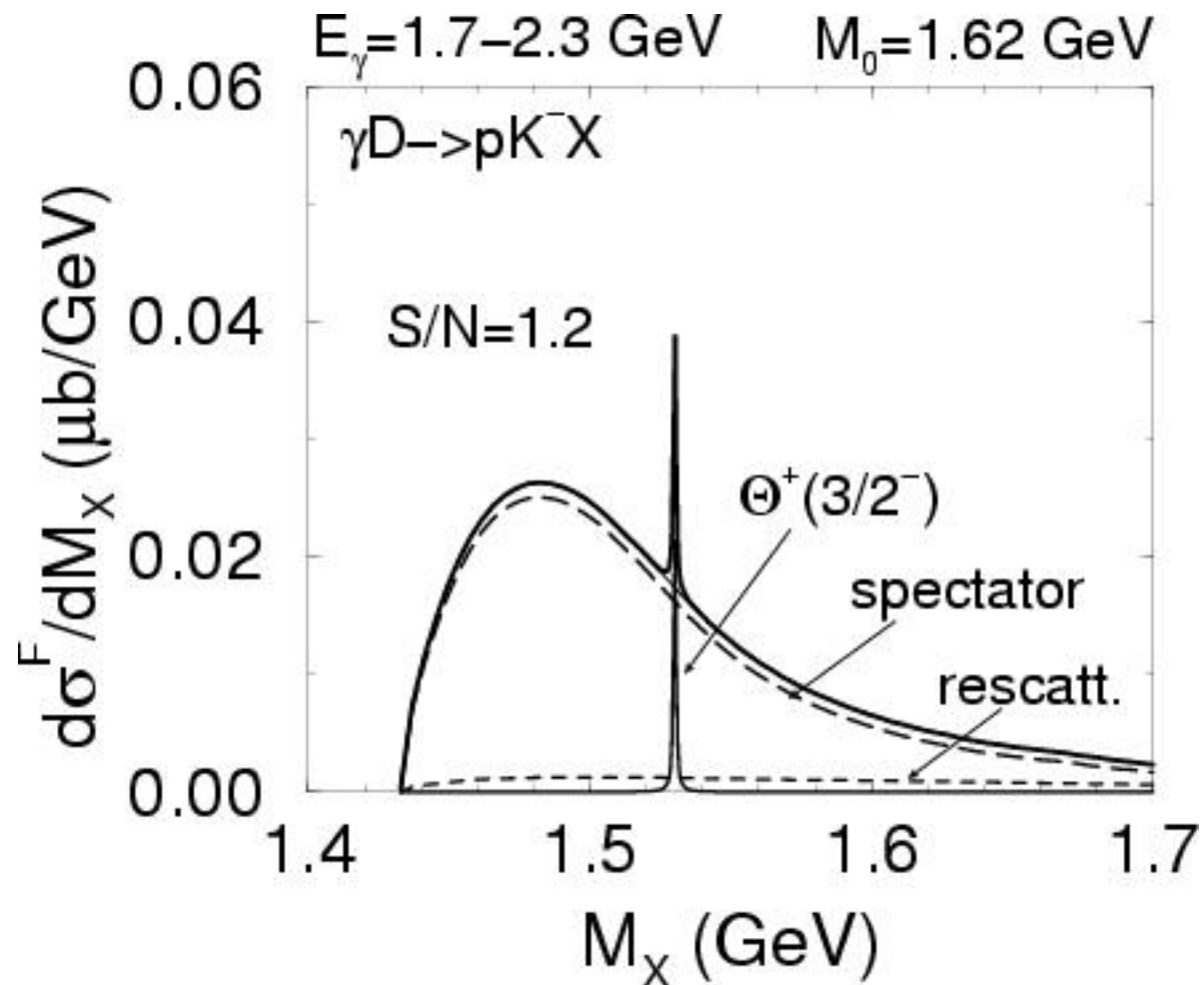
$$\theta_{\gamma, pK^-} < 22^\circ$$



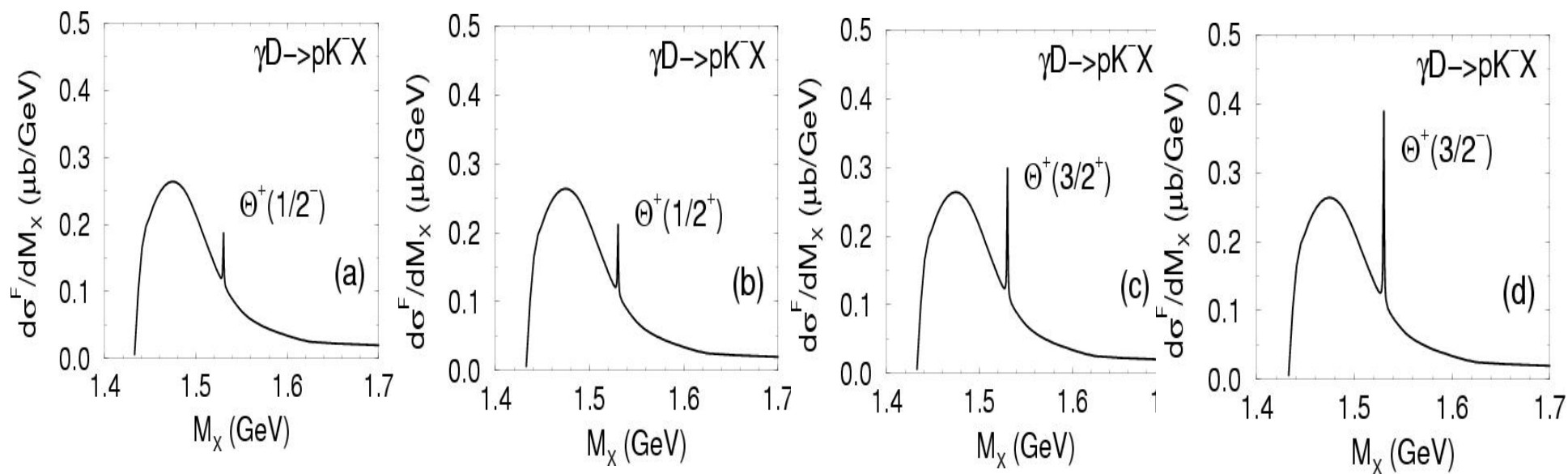
Reason of the spectrum shape modification



outside of Λ^* resonance region



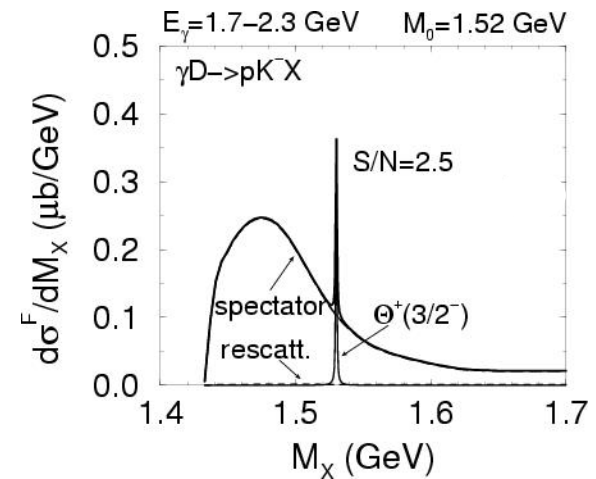
Θ^+ Spin and Parity



Total cross section
of Θ^+ photoproduction
at LEPS conditions
in $\gamma D \rightarrow \Theta^+ X$ reactions

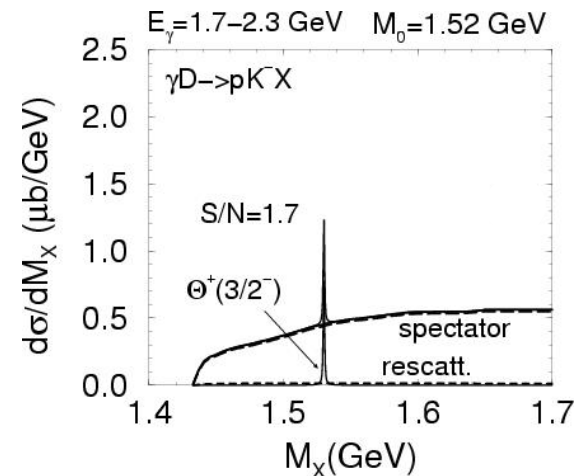
$$\left. \frac{d\sigma^{\Theta^+ F}}{dM} \right|_{\max} \simeq 0.26 \frac{\mu\text{b}}{\text{GeV}},$$

$$\sigma_{\text{tot}}^{\Theta^+ F} \simeq \frac{\pi}{2} \times \Gamma_{\Theta} \times \left. \frac{d\sigma^{\Theta^+ F}}{dM} \right|_{\max} \simeq 0.41 \text{ nb}$$



Total cross section
of Θ^+ photoproduction
in $\gamma D \rightarrow \Theta^+ X$ reactions

$$\sigma_{\text{tot}}^{\Theta^+} \simeq 1.0 \text{ nb}$$



CLAS acceptance and conditions of data analysis

Acceptance:

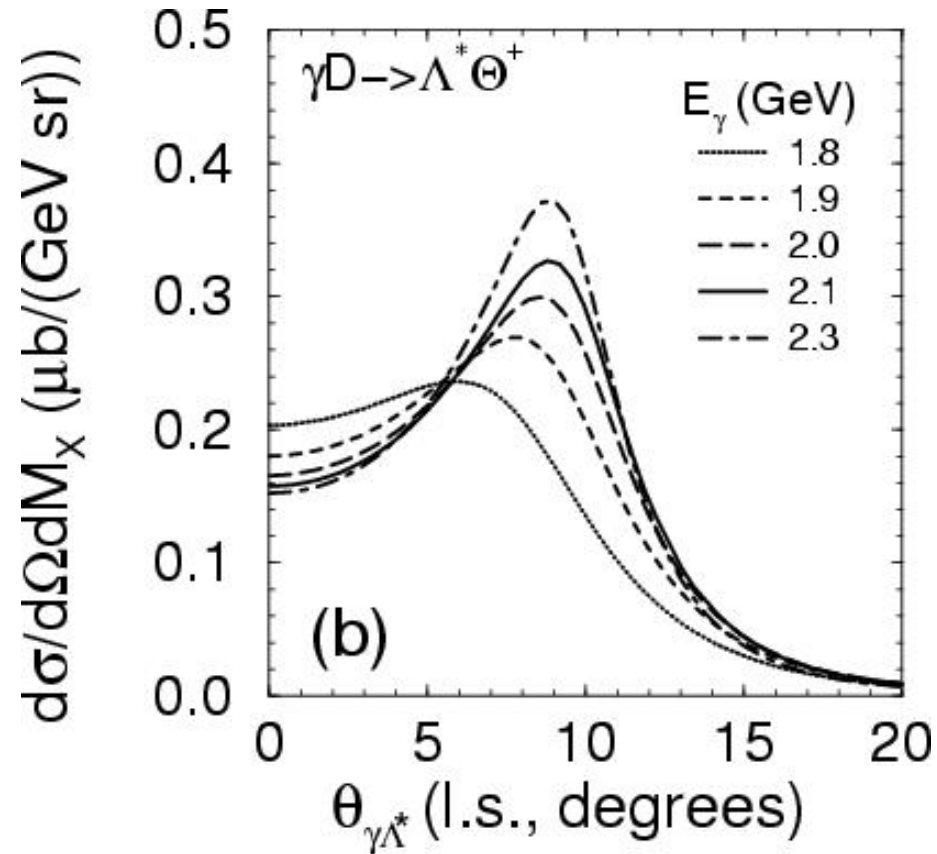
- (i) $p_p > 0.35 \text{ GeV}/c$, $p_K > 0.25 \text{ GeV}/c$
- (ii) $\theta_+ > 9^\circ$, $\theta_- > 15^\circ$

Conditions are related to purpose:

look for $\gamma n \rightarrow \Theta^+ K^-$ reaction

- (iii) ϕ meson cut $M_{K^+K^-} > 1.06 \text{ GeV}$
- (iv) Λ^* cut $|M_{pK^-} - M_{\Lambda^*}| > 25 \text{ MeV}$
- (v) neutron momentum cut $p_n > 0.2 \text{ GeV}/c$

CLAS conditions and Θ^+ signal

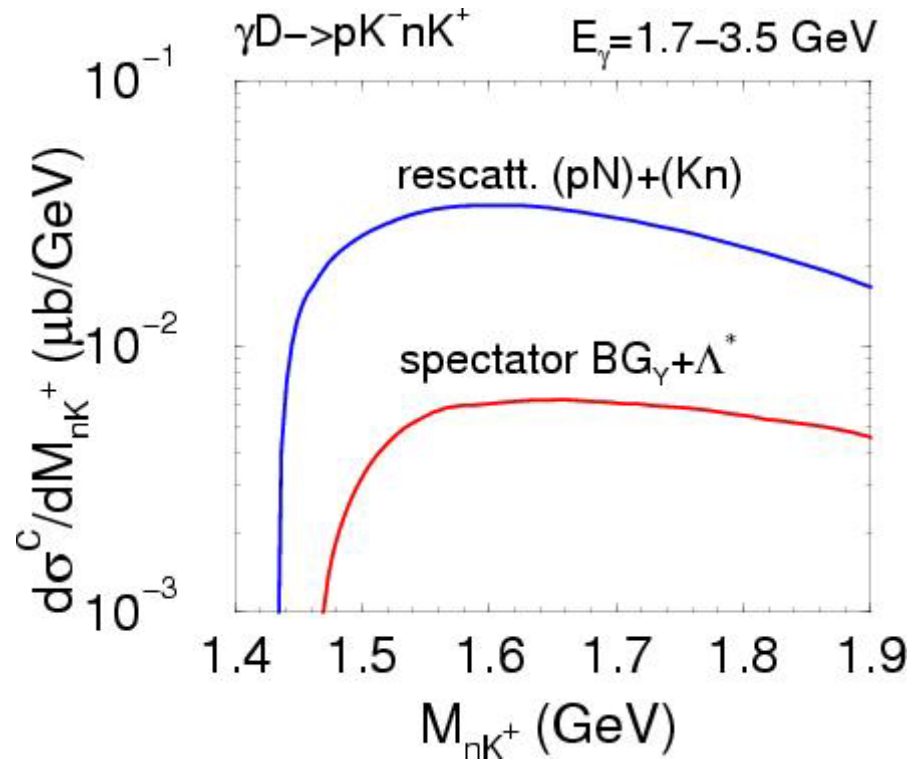


$$\theta_+ > 9^\circ, \theta_- > 15^\circ$$



Suppress the signal

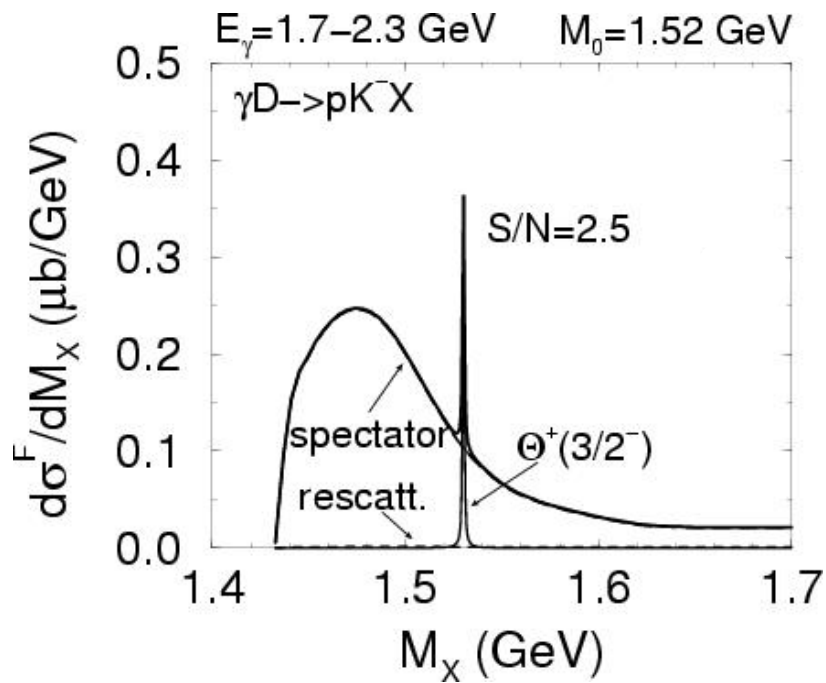
CLAS conditions and background



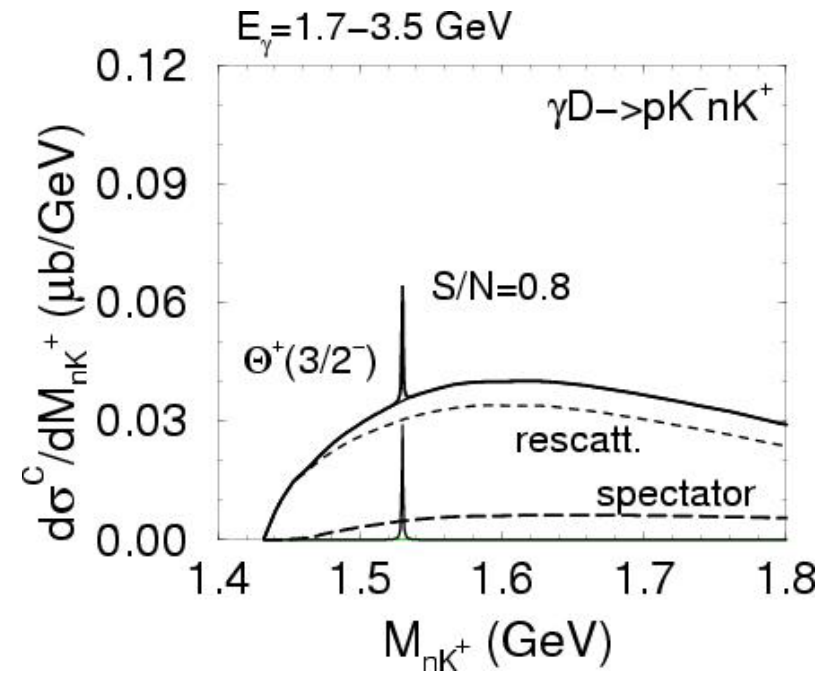
Λ^* cut $|M_{pK^-} - M_{\Lambda^*}| > 25$ MeV

neutron momentum cut $p_n > 0.2$ GeV/c

LEPS conditions



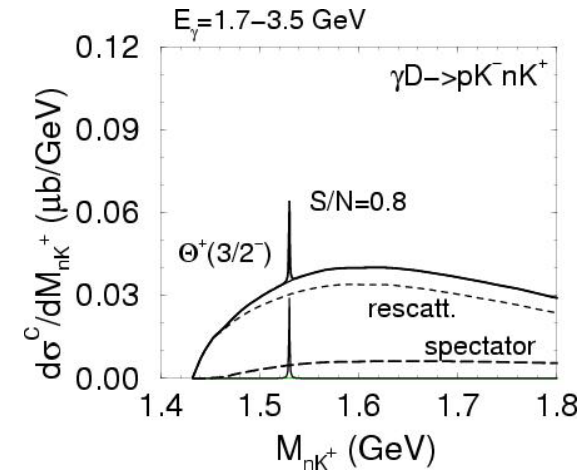
CLAS conditions



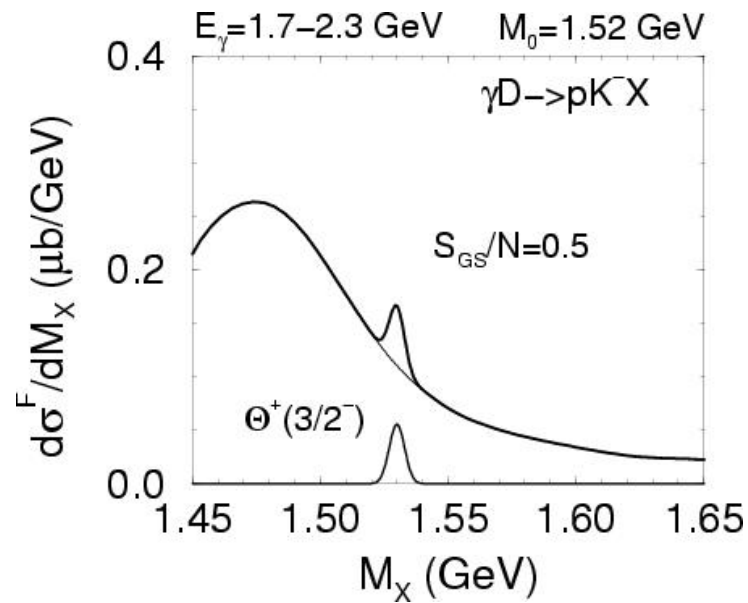
Total cross section
of Θ^+ photoproduction
at CLAS conditions
in $\gamma D \rightarrow \Theta^+ X$ reactions

$$\frac{d\sigma^{\Theta^+ C}}{dM} \Big|_{\max} \simeq 42 \frac{\text{nb}}{\text{GeV}},$$

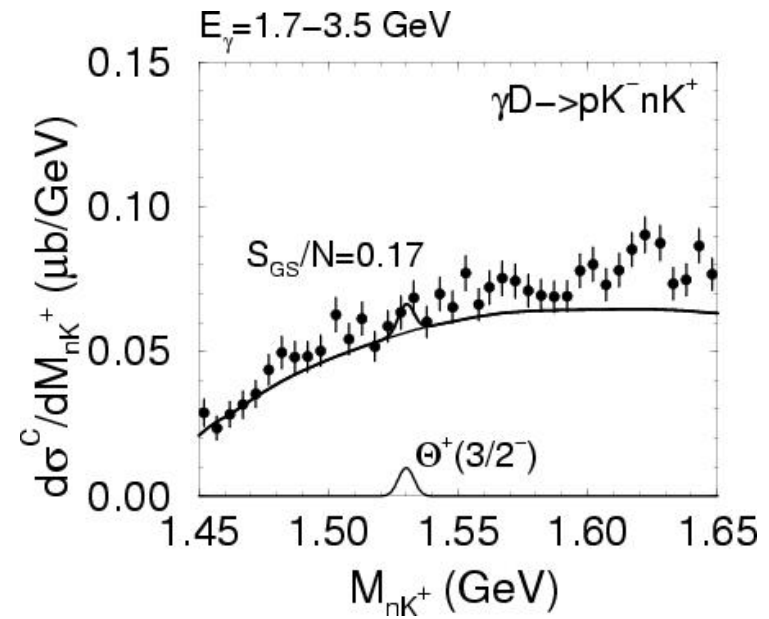
$$\sigma_{\text{tot}}^{\Theta^+ C} \simeq 2 \times \frac{\pi}{2} \times \Gamma_{\Theta} \times \frac{d\sigma^{\Theta^+ F}}{dM} \Big|_{\max} \simeq 0.13 \text{ nb}$$



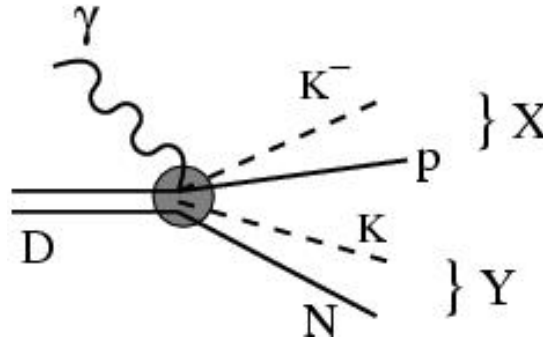
LEPS conditions



CLAS conditions



Acceptance correction



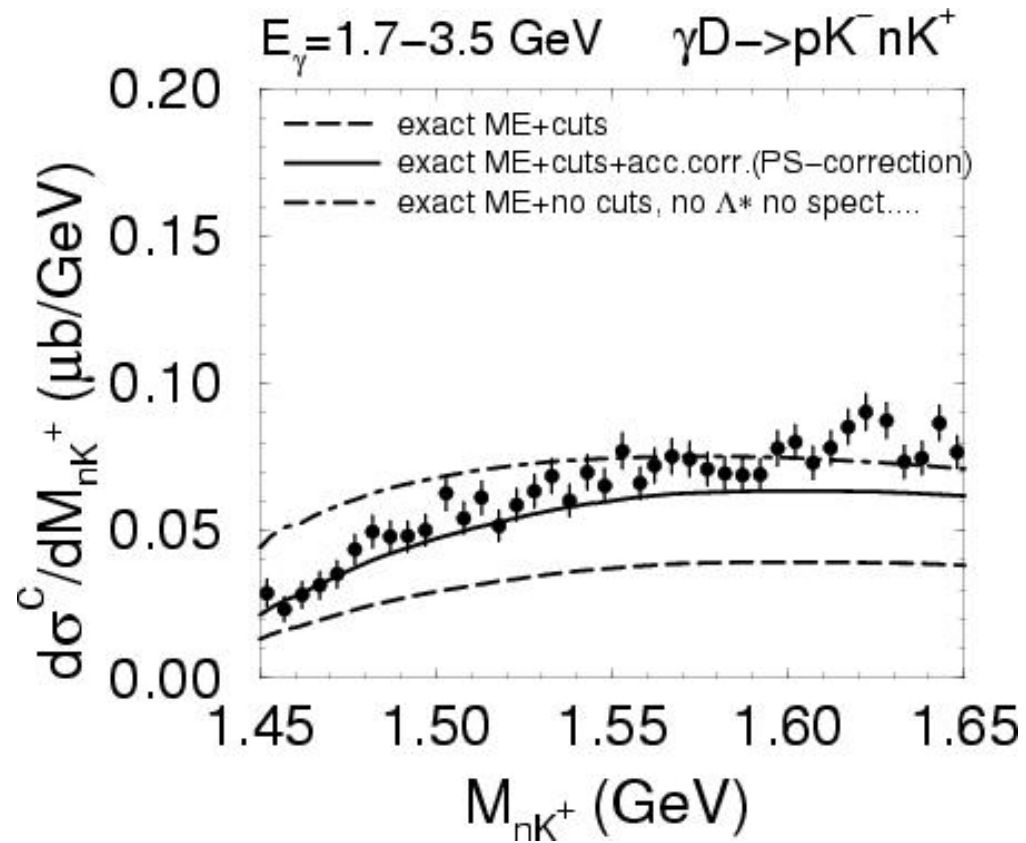
$$\frac{d\sigma}{dM_Y} = 2\pi \int \frac{d\sigma}{d[\dots]} dM_X d\cos\theta_X$$

$$\times \frac{1}{64\pi^2 s_D} \frac{p_f}{p_i} \frac{1}{6} \sum_{[fi]} |T_{fi}|^2 \frac{\bar{q}' d\Omega_{\bar{q}'}}{16\pi^3} \frac{q' d\Omega_{q'}}{16\pi^3} \quad 6 \text{ dimensional integral}$$

$$dM_X d\cos\theta d\Omega_X d\Omega_Y \rightarrow dM_X dp_n dp_{K^+} d\cos\theta_{K^+} d\cos\theta_{K^-} d\cos\theta_p$$

$$\frac{V}{V_{\text{cut}}} \simeq \frac{1^6}{(1-0.05)^6} \simeq 1.4$$

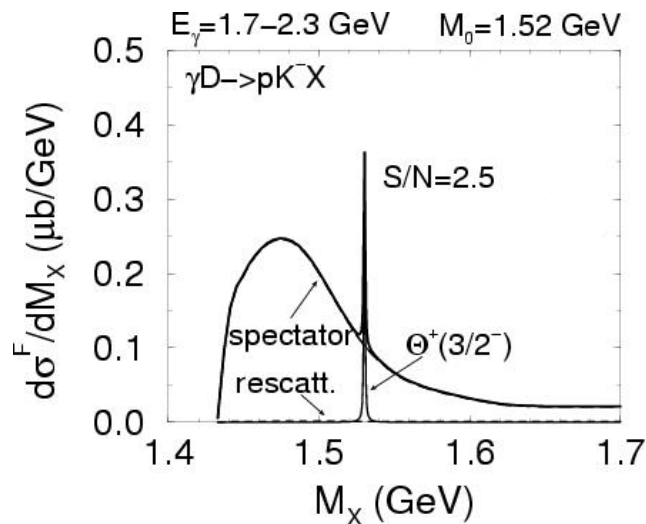
Acceptance correction



Summary

Preferable conditions for Θ^+ formation process

1. **Reaction** $\gamma D \rightarrow pK^- X$
2. pK^- pair is detected at forward direction
with $\theta_{\gamma, pK^- \text{ lab.}} \leq 9 - 10^\circ$
3. Mass of pK^- pair is close to M_{Λ^*}
4. **Photon energy** $E_\gamma \sim 2.0 - 2.2 \text{ GeV}$



↓ LD₂ data (preliminary)
 $1.50 < M(pK^-) < 1.54 \text{ GeV}/c^2$

MMd(γ, pK^-) GeV/c²